Fifth Edition

Structural Analysis

Aslam Kassimali

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Aslam Kassimali

Southern Illinois University-Carbondale



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Structural Analysis, Fifth Edition Aslam Kassimali

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Contents

Preface xiii About the Author xvii

PART 1 INTRODUCTION TO STRUCTURAL ANALYSIS AND LOADS 1

1	Introduction to Structural Analysis	3
	1.1	Historical Background 3
	1.2	Role of Structural Analysis in Structural Engineering Projects 5
	1.3	Classification of Structures 7
	1.4	Analytical Models 12
		Summary 16
2	Loads on Structures 17	
	2.1	Structural Systems for Transmitting Loads 18
	2.2	Dead Loads 29
	2.3	Live Loads 31
	2.4	Classification of Buildings for Environmental Loads 34
	2.5	Wind Loads 34
	2.6	Snow Loads 42
	2.7	Earthquake Loads 45
	2.8	Hydrostatic and Soil Pressures 46
	2.9	Thermal and Other Effects 46
	2.10	Load Combinations 47
		Summary 48

PART 2 ANALYSIS OF STATICALLY DETERMINATE STRUCTURES 51

3	Equilibrium and Support Reactions	53	
	3.1		Equilibrium of Structures 53
	3.2		External and Internal Forces 56
	3.3		Types of Supports for Plane Structures 56
	3.4		Static Determinacy, Indeterminacy, and Instability 58
	3.5		Computation of Reactions 69
	3.6		Principle of Superposition 85
	3.7		Reactions of Simply Supported Structures Using Proportions 86
			Summary 88
			Problems 89
4	Plane and Space Trusses 97		

4.1	Assumptions for Analysis of Trusses 99
4.2	Arrangement of Members of Plane Trusses—Internal Stability 103
4.3	Equations of Condition for Plane Trusses 107
4.4	Static Determinacy, Indeterminacy, and Instability of Plane Trusses 107
4.5	Analysis of Plane Trusses by the Method of Joints 113
4.6	Analysis of Plane Trusses by the Method of Sections 126
4.7	Analysis of Compound Trusses 132
4.8	Complex Trusses 137
4.9	Space Trusses 138
	Summary 147
	Problems 148

5	Beams and Frames: Shear and Bending Mor	Beams and Frames: Shear and Bending Moment 161				
	5.1 A:	xial Force, Shear, and Bending Moment 161				
	5.2 Sh	ear and Bending Moment Diagrams 168				
	5.3 Q	ualitative Deflected Shapes 172				
	5.4 Re M	elationships between Loads, Shears, and Bending oments 173				
	5.5 St F1	atic Determinacy, Indeterminacy, and Instability of Plane rames 192				

5.6 Analysis of Plane Frames 200 Summary 213 Problems 215

6	Deflections of Beams: Geometric Metho	ods 224
	6.1	Differential Equation for Beam Deflection 225
	6.2	Direct Integration Method 227
	6.3	Superposition Method 231
	6.4	Moment-Area Method 231
	6.5	Bending Moment Diagrams by Parts 243
	6.6	Conjugate-Beam Method 247
		Summary 262
		Problems 262

7	Deflections of Trusses, Beams, and Frames: Work–Energy Methods 268			
	7.1	Work 268		
	7.2	Principle of Virtual Work 270		
	7.3	Deflections of Trusses by the Virtual Work Method 274		
	7.4	Deflections of Beams by the Virtual Work Method 283		
	7.5	Deflections of Frames by the Virtual Work Method 295		
	7.6	Conservation of Energy and Strain Energy 306		
	7.7	Castigliano's Second Theorem 309		
	7.8	Betti's Law and Maxwell's Law of Reciprocal Deflections 317		
		Summary 319		
		Problems 320		

8	Influence Lines 329		
		8.1	Influence Lines for Beams and Frames by Equilibrium Method 330
		8.2	Müller-Breslau's Principle and Qualitative Influence Lines 344
		8.3	Influence Lines for Girders with Floor Systems 356
		8.4	Influence Lines for Trusses 366
		8.5	Influence Lines for Deflections 377
			Summary 380
			Problems 380
9	Application of Influence Lines	387	

9.1	Respons	se at a	Part	ticula	r Lo	cation	1 Due	e to a	a Single	Movi	ing
	Concent	rated	Load	d 387	7						
~ ~	D		D	• •	т	. •	D		TT :C	1	

9.2 Response at a Particular Location Due to a Uniformly Distributed Live Load 389

- 9.3 Response at a Particular Location Due to a Series of Moving Concentrated Loads 393
- 9.4 Absolute Maximum Response 400 Summary 405 Problems 406

10 Analysis of Symmetric Structures 408

10.1	Symmetric Structures 408
10.2	Symmetric and Antisymmetric Components of Loadings 414
10.3	Behavior of Symmetric Structures under Symmetric and Antisymmetric Loadings 424
10.4	Procedure for Analysis of Symmetric Structures 428
	Summary 435
	Problems 436

PART 3 ANALYSIS OF STATICALLY INDETERMINATE STRUCTURES 439

11	Introduction to Statically Indeterminate Structures 441				
	11.1	Advantages and Disadvantages of Indeterminate Structures 442			
	11.2	Analysis of Indeterminate Structures 445			
		Summary 449			
12	Approximate Analysis of Rectangular Building Frames 450				
	12.1	Assumptions for Approximate Analysis 451			
	12.2	Analysis for Vertical Loads 454			
	12.3	Analysis for Lateral Loads—Portal Method 458			
	12.4	Analysis for Lateral Loads—Cantilever Method 473			
		Summary 480			
		Problems 480			
13	Method of Consistent Deformations—Force Method 483				
	13.1	Structures with a Single Degree of Indeterminacy 484			
	13.2	Internal Forces and Moments as Redundants 504			
	13.3	Structures with Multiple Degrees of Indeterminacy 515			
	13.4	Support Settlements, Temperature Changes, and Fabrication Errors 537			
	13.5	Method of Least Work 545			
		Summary 551			
		Problems 552			

14	Influence Lines for Statically Indeterminate Structures 559				
		14.1	Influence Lines for Beams and Trusses 560		
		14.2	Qualitative Influence Lines by Müller-Breslau's Principle 575		
			Summary 579		
			Problems 580		
15	Slope-Deflection Method 5	83			
		15.1	Slope-Deflection Equations 584		
		15.2	Basic Concept of the Slope-Deflection Method 591		
		15.3	Analysis of Continuous Beams 598		
		15.4	Analysis of Frames without Sidesway 617		
		15.5	Analysis of Frames with Sidesway 625		
			Summary 643		
			Problems 643		
16	Moment-Distribution Method 648				
		16.1	Definitions and Terminology 649		
		16.2	Basic Concept of the Moment-Distribution Method 657		
		16.3	Analysis of Continuous Beams 665		
		16.4	Analysis of Frames without Sidesway 678		
		16.5	Analysis of Frames with Sidesway 681		
			Summary 696		
			Problems 697		
17	Introduction to Matrix Struct	ural Analys	sis 702		
		17.1	Analytical Model 703		
		17.2	Member Stiffness Relations in Local Coordinates 707		
		17.3	Coordinate Transformations 714		
		17.4	Member Stiffness Relations in Global Coordinates 719		
		17.5	Structure Stiffness Relations 721		
		17.6	Procedure for Analysis 728		
			Summary 745		
			Problems 745		

APPENDIX A Areas and Centroids of Geometric Shapes 747

xii Contents

APPENDIX B	Review of Matrix Algebra	749	
		B.1	Definition of a Matrix 749
		B.2	Types of Matrices 750
		B.3	Matrix Operations 752
		B.4	Solution of Simultaneous Equations by the Gauss-Jordan Method 758
			Problems 762
APPENDIX C	Computer Software 763	}	
		C.1	Starting the Computer Software 763
		C.2	Inputting Data 763
		C.3	Results of the Analysis 769
			Problems 774
APPENDIX D	Three-Moment Equation	775	
		D.1	Derivation of Three-Moment Equation 775
		D.2	Application of Three-Moment Equation 780
			Summary 786
			Problems 787
		Biblio	graphy 789
		Answe	ers to Selected Problems 791
		Index	801



Preface

The objective of this book is to develop an understanding of the basic principles of structural analysis. Emphasizing the intuitive classical approach, *Structural Analysis* covers the analysis of statically determinate and indeterminate beams, trusses, and rigid frames. It also presents an introduction to the matrix analysis of structures.

The book is divided into three parts. Part One presents a general introduction to the subject of structural engineering. It includes a chapter devoted entirely to the topic of loads because attention to this important topic is generally lacking in many civil engineering curricula. Part Two, consisting of Chapters 3 through 10, covers the analysis of statically determinate beams, trusses, and rigid frames. The chapters on deflections (Chapters 6 and 7) are placed before those on influence lines (Chapters 8 and 9), so that influence lines for deflections can be included in the latter chapters. This part also contains a chapter on the analysis of symmetric structures (Chapter 10). Part Three of the book, Chapters 11 through 17, covers the analysis of statically indeterminate structures. The format of the book is flexible to enable instructors to emphasize topics that are consistent with the goals of the course.

Each chapter of the book begins with an introductory section defining its objective and ends with a summary section outlining its salient features. An important general feature of the book is the inclusion of step-by-step procedures for analysis to enable students to make an easier transition from theory to problem solving. Numerous solved examples are provided to illustrate the application of the fundamental concepts.

A computer program for analyzing plane framed structures is available on the publisher's website www.cengage.com/engineering. This interactive software can be used to simulate a variety of structural and loading configurations and to determine cause versus effect relationships between loading and various structural parameters, thereby enhancing the students' understanding of the behavior of structures. The software shows deflected shapes of structures to enhance students' understanding of structural response due to various types of loadings. It can also include the effects of support settlements, temperature changes, and fabrication errors in the analysis. A solutions manual, containing complete solutions to over 600 text exercises, is also available for the instructor.

New to the Fifth Edition

Building upon the original theme of this book which is that detailed explanations of concepts provide the most effective means of teaching structural analysis, the following improvements and changes have been made in this fifth edition:

- The entire artwork for the book has been redrawn in two colors to enhance clarity. Where applicable, the external loading and reactions of the structure, as well as its deformed (deflected) shape, are shown in blue; whereas, the undeformed structure, its supports and dimensions are drawn in black/grey.
- A new section on structural systems for transmitting loads has been added in Chapter 2, where the concepts of gravity and lateral load paths and tributary areas are introduced. Also in this chapter, the previously separate sections on live loads and impact have now been combined, another new section on the classification of buildings for environmental loads as per ASCE/SEI 7-10 Standard has been added, and all the material on loads has been revised to meet the provisions of this latest version of the ASCE/SEI 7 Standard.
- In chapter 7, the treatment of the virtual work method has been expanded by including a graphical procedure for evaluating the virtual work integrals, along with two new examples to illustrate the application of this procedure.
- Based on reviewers' input, Chapter 14 of the previous edition has been deleted, with the method of least work now covered in Chapter 13 and the treatment of the three-moment equation moved to a new Appendix D. The subsequent chapters of the book have been re-numbered accordingly.
- Over 15 percent of the problems from the previous edition have been replaced with new ones.
- There are numerous other minor revisions, including an expanded discussion of static determinacy of trusses (Chapter 4), and addition of new photographs and figures illustrating some typical building frame connections (Chapter 5). The page layout has been redesigned to enhance clarity. Finally, the computer software has been upgraded and recompiled to make it compatible with the latest versions of Microsoft Windows.

Ancillaries for the Fifth Edition

Worked-out solutions to all end-of-chapter problems are provided in the Instructors Solutions Manual, and available in print or digitally to registered instructors on the instructor resources web site. Two sets of PowerPoint slides, one of all figures and tables, the other of examples and equations to allow instructors an easier way to prepare their lectures, are also available on the instructor website, at www.cengage .com/engineering. The computer software program is available for students using the text, through www.cengagebrain.com, and for instructors through either site.

MindTap Online Course and Reader

In addition to the print version, this textbook will also be available online through MindTap, a personalized learning program. Students who purchase the MindTap version will have access to the book's MindTap Reader and will be able to complete homework and assessment material online, through their desktop, laptop, or iPad. If your class is using a Learning Management System (such as Blackboard, Moodle, or Angel) for tracking course content, assignments, and grading, you can seamlessly access the MindTap suite of content and assessments for this course.

In MindTap, instructors can:

- Personalize the Learning Path to match the course syllabus by rearranging content, hiding sections, or appending original material to the textbook content
- Connect a Learning Management System portal to the online course and Reader
- Customize online assessments and assignments
- Track student progress and comprehension with the Progress app
- Promote student engagement through interactivity and exercises

Additionally, students can listen to the text through ReadSpeaker, take notes and highlight content for easy reference, and check their understanding of the material.

Acknowledgments

I wish to express my thanks to Timothy Anderson and Hilda Gowans of Cengage Learning for their constant support and encouragement throughout this project, and to Rose Kernan for all her help during the production phase. The comments and suggestions for improvement from colleagues and students who have used previous editions are gratefully acknowledged. All of their suggestions were carefully considered, and implemented whenever possible. Thanks are due to the following reviewers for their careful reviews of the manuscripts of the various editions, and for their constructive suggestions:

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Finally, I would like to express my loving appreciation to my wife, Maureen, for her constant encouragement and help in preparing this manuscript, and to my sons, Jamil and Nadim, for their love, understanding and patience.

Aslam Kassimali



About the Author

Aslam Kassimali was born in Karachi, Pakistan. He received his Bachelor of Engineering (B.E.) degree in civil engineering from the University of Karachi (N.E.D. College) in Pakistan in 1969. In 1971, he earned a Master of Engineering (M.E.) degree in civil engineering from Iowa State University in Ames, Iowa, USA. After completing further studies and research at the University of Missouri at Columbia in the USA, he received Master of Science (M.S.) and Ph.D. degrees in civil engineering in 1974 and 1976, respectively.

His practical experience includes work as a Structural Design Engineer for Lutz, Daily and Brain, Consulting Engineers, Shawnee Mission, Kansas (USA), from January to July 1973, and as a Structural Engineering Specialist and Analyst for Sargent & Lundy Engineers in Chicago, Illinois (USA) from 1978 to 1980. He joined Southern Illinois University – Carbondale (USA) as an Assistant Professor in 1980, and was promoted to the rank of Professor in 1993. Consistently recognized for teaching excellence, Dr. Kassimali has received over 20 awards for outstanding teaching at Southern Illinois University-Carbondale, and was awarded the title of Distinguished Teacher in 2004. He is currently a Professor and Distinguished Teacher in the Department of Civil & Environmental Engineering at Southern Illinois University in Carbondale, Illinois (USA). He has authored and co-authored four textbooks on structural analysis and mechanics, and has published a number of papers in the area of nonlinear structural analysis.

Dr. Kassimali is a life member of the American Society of Civil Engineers (ASCE), and has served on the ASCE Structural Division Committees on *Shock and Vibratory Effects, Special Structures,* and *Methods of Analysis.*



Part One Introduction to Structural Analysis and Loads



Marina City District, Chicago Hisham Ibrahim / Photographer's Choice RF /Getty Images

Introduction to Structural Analysis

- 1.1 Historical Background
- **1.2** Role of Structural Analysis in Structural Engineering Projects
- 1.3 Classification of Structures1.4 Analytical Models
 - Summary

Structural analysis is the prediction of the performance of a given structure under prescribed loads and/or other external effects, such as support movements and temperature changes. The performance characteristics commonly of interest in the design of structures are (1) stresses or stress resultants, such as axial forces, shear forces, and bending moments; (2) deflections; and (3) support reactions. Thus, the analysis of a structure usually involves determination of these quantities as caused by a given loading condition. The objective of this text is to present the methods for the analysis of structures in static equilibrium.

This chapter provides a general introduction to the subject of structural analysis. We first give a brief historical background, including names of people whose work is important in the field. Then we discuss the role of structural analysis in structural engineering projects. We describe the five common types of structures: tension and compression structures, trusses, and shear and bending structures. Finally, we consider the development of the simplified models of real structures for the purpose of analysis.

1.1 Historical Background

Since the dawn of history, structural engineering has been an essential part of human endeavor. However, it was not until about the middle of the seventeenth century that engineers began applying the knowledge of mechanics (mathematics and science) in designing structures. Earlier engineering structures were designed by trial and error and by using rules of thumb based on past experience. The fact that some of the magnificent structures from earlier eras, such as Egyptian pyramids (about 3000 B.C.), Greek temples (500–200 B.C.), Roman coliseums and aqueducts (200 B.C.–A.D. 200), and Gothic cathedrals (A.D. 1000–1500), still stand today is a testimonial to the ingenuity of their builders (Fig. 1.1).

Galileo Galilei (1564–1642) is generally considered to be the originator of the theory of structures. In his book entitled *Two New Sciences*, which was published in 1638, Galileo analyzed the failure of some simple structures, including cantilever beams. Although Galileo's predictions of strengths of beams were only approximate, his work laid the foundation for future developments in the theory of structures and ushered in a new era of structural engineering, in which the analytical principles of mechanics and strength of materials would have a major influence on the design of structures.

Following Galileo's pioneering work, the knowledge of structural mechanics advanced at a rapid pace in the second half of the seventeenth century and into the eighteenth century. Among the notable investigators of that period were Robert Hooke (1635–1703), who developed the law of linear relationships between the force and deformation of materials (Hooke's law); Sir Isaac Newton (1642–1727), who formulated the laws of motion and developed calculus; John Bernoulli (1667–1748), who formulated the principle of virtual work; Leonhard Euler (1707–1783), who developed the theory of buckling of columns; and



FIG. 1.1 The Cathedral of Notre Dame in Paris was Completed in the Thirteenth Century Ritu Manoj Jethani / Shutterstock.com C. A. de Coulomb (1736–1806), who presented the analysis of bending of elastic beams.

In 1826 L. M. Navier (1785-1836) published a treatise on elastic behavior of structures, which is considered to be the first textbook on the modern theory of strength of materials. The development of structural mechanics continued at a tremendous pace throughout the rest of the nineteenth century and into the first half of the twentieth, when most of the classical methods for the analysis of structures described in this text were developed. The important contributors of this period included B. P. Clapeyron (1799–1864), who formulated the three-moment equation for the analysis of continuous beams; J. C. Maxwell (1831–1879), who presented the method of consistent deformations and the law of reciprocal deflections; Otto Mohr (1835–1918), who developed the conjugate-beam method for calculation of deflections and Mohr's circles of stress and strain; Alberto Castigliano (1847-1884), who formulated the theorem of least work; C. E. Greene (1842–1903), who developed the moment-area method; H. Muller-Breslau (1851-1925), who presented a principle for constructing influence lines: G. A. Maney (1888–1947), who developed the slope-deflection method, which is considered to be the precursor of the matrix stiffness method; and Hardy Cross (1885-1959), who developed the moment-distribution method in 1924. The moment-distribution method provided engineers with a simple iterative procedure for analyzing highly statically indeterminate structures. This method, which was the most widely used by structural engineers during the period from about 1930 to 1970, contributed significantly to their understanding of the behavior of statically indeterminate frames. Many structures designed during that period, such as high-rise buildings, would not have been possible without the availability of the moment-distribution method.

The availability of computers in the 1950s revolutionized structural analysis. Because the computer could solve large systems of simultaneous equations, analyses that took days and sometimes weeks in the precomputer era could now be performed in seconds. The development of the current computer-oriented methods of structural analysis can be attributed to, among others, J. H. Argyris, R. W. Clough, S. Kelsey, R. K. Livesley, H. C. Martin, M. T. Turner, E. L. Wilson, and O. C. Zienkiewicz.

1.2 Role of Structural Analysis in Structural Engineering Projects

Structural engineering is the science and art of planning, designing, and constructing safe and economical structures that will serve their intended purposes. Structural analysis is an integral part of any structural engineering project, its function being the prediction of the performance of the proposed structure. A flowchart showing the various phases of a typical structural engineering project is presented in Fig. 1.2. As this diagram indicates, the process is an iterative one, and it generally consists of the following steps:

1. *Planning Phase* The planning phase usually involves the establishment of the functional requirements of the proposed structure, the general layout and dimensions of the structure, consideration of the possible types of structures (e.g., rigid frame



FIG. 1.2 Phases of a Typical Structural Engineering Project

or truss) that may be feasible and the types of materials to be used (e.g., structural steel or reinforced concrete). This phase may also involve consideration of nonstructural factors, such as aesthetics, environmental impact of the structure, and so on. The outcome of this phase is usually a structural system that meets the functional requirements and is expected to be the most economical. This phase is perhaps the most crucial one of the entire project and requires experience and knowledge of construction practices in addition to a thorough understanding of the behavior of structures.

- 2. *Preliminary Structural Design* In the preliminary structural design phase, the sizes of the various members of the structural system selected in the planning phase are estimated based on approximate analysis, past experience, and code requirements. The member sizes thus selected are used in the next phase to estimate the weight of the structure.
- **3.** *Estimation of Loads* Estimation of loads involves determination of all the loads that can be expected to act on the structure.
- **4.** *Structural Analysis* In structural analysis, the values of the loads are used to carry out an analysis of the structure in order to determine the stresses or stress resultants in the members and the deflections at various points of the structure.
- 5. *Safety and Serviceability Checks* The results of the analysis are used to determine whether or not the structure satisfies the

safety and serviceability requirements of the design codes. If these requirements are satisfied, then the design drawings and the construction specifications are prepared, and the construction phase begins.

6. *Revised Structural Design* If the code requirements are not satisfied, then the member sizes are revised, and phases 3 through 5 are repeated until all the safety and serviceability requirements are satisfied.

Except for a discussion of the types of loads that can be expected to act on structures (Chapter 2), our primary focus in this text will be on the analysis of structures.

1.3 Classification of Structures

As discussed in the preceding section, perhaps the most important decision made by a structural engineer in implementing an engineering project is the selection of the type of structure to be used for supporting or transmitting loads. Commonly used structures can be classified into five basic categories, depending on the type of primary stresses that may develop in their members under major design loads. However, it should be realized that any two or more of the basic structural types described in the following may be combined in a single structure, such as a building or a bridge, to meet the structure's functional requirements.

Tension Structures

The members of tension structures are subjected to pure tension under the action of external loads. Because the tensile stress is distributed uniformly over the cross-sectional areas of members, the material of such a structure is utilized in the most efficient manner. Tension structures composed of flexible steel cables are frequently employed to support bridges and long-span roofs. Because of their flexibility, cables have negligible bending stiffness and can develop only tension. Thus, under external loads, a cable adopts a shape that enables it to support the load by tensile forces alone. In other words, the shape of a cable changes as the loads acting on it change. As an example, the shapes that a single cable may assume under two different loading conditions are shown in Fig. 1.3.

Figure 1.4 shows a familiar type of cable structure—the *suspension bridge*. In a suspension bridge, the roadway is suspended from two main cables by means of vertical hangers. The main cables pass over a pair of towers and are anchored into solid rock or a concrete foundation at their ends. Because suspension bridges and other cable structures lack stiffness in lateral directions, they are susceptible to wind-induced oscillations (see Fig. 1.5). Bracing or stiffening systems are therefore provided to reduce such oscillations.

Besides cable structures, other examples of tension structures include vertical rods used as hangers (for example, to support balconies or tanks) and membrane structures such as tents and roofs of large-span domes (Fig. 1.6).









FIG. 1.4 Suspension Bridge

FIG. 1.5 Tacoma Narrows Bridge Oscillating before Its Collapse in 1940 Smithsonian Institution Photo No. 72-787. Division of Work & Industry, National Museum of American History, Smithsonian Institution



FIG. 1.6 The Fabric (membrane) Roof of the Tokyo Dome is Tensioned (inflated) by Air Pressure from Inside the Stadium © Gavin Hellier / Alamy

Compression Structures

Compression structures develop mainly compressive stresses under the action of external loads. Two common examples of such structures are *columns* and *arches* (Fig. 1.7). Columns are straight members subjected to axially compressive loads, as shown in Fig. 1.8. When a straight member is subjected to lateral loads and/or moments in addition to axial loads, it is called a *beam-column*.

An arch is a curved structure, with a shape similar to that of an inverted cable, as shown in Fig. 1.9. Such structures are frequently used



FIG. 1.7 Columns and Arches of the Segovia (Roman) Aqueduct Bridge in Spain (constructed in the first or the second centuries) Bluedog423